Modeling Thermal Radiation in Open Liquid Pool Fires

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ABSTRACT

A non-isothermal, non-homogeneous approach has been developed for radiation analysis of moderate to large scale liquid pool fires, with a special emphasis on soot formation and the absorption and emission processes. The present field approach reveals the phenomenon of radiative energy blockage by the cold fuel and soot particles in the vicinity of the fuel bed, resulting in a variable heat flux distribution at the fuel surface. The convective contribution to the heat feedback at the fuel surface is found to decrease from 54 to 5% as the pool diameter increases from 15 to 50 cm, while the radiative contribution proportionately increases. The estimated mass evaporation rate and the total radiative output from the flame agree closely with experiment.

INTRODUCTION

Current interests in the thermal radiation behavior of pool fires exists primarily because of its importance in controlling the mass burning rate and overall fire hazard of moderate to large scale pool fires [1]. In a sooting flame, radiation is strongly affected by the soot absorption process. In such flames, the maximum energy feedback has been postulated to come from the bottom 20-30% of the flame height [1]. The vicinity of the flame base comprises basically the cold fuel vapor and the soot particles. Hence a precise knowledge of the spatial distribution of the gaseous species, soot particles, and the temperature is necessary for a quantitative estimation of the flame radiation to the fuel surface.

The previous work on radiation analysis has been reported by de Ris [1], Modak [2], Markstein [3,4], and Brosmer and Tein [5]. These models were of varying degrees of complexity. For example, most of the previous models include the mean beam length approach combined with the uniform, isothermal, gray gas absorption approximation. However, the importance of non-gray, non-isothermal, and non-homogeneous effects in sooty fires of moderate scale has been shown by Buckius and Tein [6]. The recent studies by Brosmer and Tein [5] considered the radiative energy blockage by the cold fuel vapor at the vicinity of the burning fuel surface.

The objective of the present work is to carry out a comprehensive analysis of the thermal radiation problem in a sooting liquid fuel fire of practical interests, such as the kerosene type of hydrocarbon fuels. The approach involves an estimation of the velocity and various scalar quantities in the flame with a special emphasis on soot formation, the
smoking tendency of the flame, and the thermal radiation from various parts of the flame both to the fuel source (feedback) and its surroundings. A four flux model is incorporated into the finite difference scheme of the main flame calculation. The model is developed with a concern for computational economy, and to provide a basic understanding of the physics, and the transport and turbulence processes.

THEORY

Flow and Turbulence

The conservation expressions for all of the variables are written in the parabolic form (Favre-averaged), for an axi-symmetric flame. A $\kappa$-$\varepsilon$ turbulence model and soot formation schemes are incorporated into the model. The details of the mathematical formulation can be found elsewhere [7-9]. This model formulation has been thoroughly tested and validated using pool-like gas flames of propane [8] and methane [9]. The model provides good predictions of the centerline temperature, velocity and species distributions, the air entrainment behavior, and the radiative and convective feedback fluxes [8,9] for these pool-like gas flames. However, the radial expansion of the flame was underestimated, particularly near the flame base. This apparently arises because of the parabolic flow assumption. The lateral pressure gradient is known to cause an elliptic effect near the flame base. Our more recent work clearly indicates this behavior [9].

The initial conditions for $\kappa$ and $\varepsilon$ in the $\kappa$-$\varepsilon$ model were introduced at the burner exit by employing the relations, $\kappa_0 = \alpha_{\kappa} U_0^2$ and $\varepsilon_0 = \alpha_{\varepsilon} \kappa^{3/2}$ /r, where r is the pool radius and $\alpha_{\kappa}$ = 10 and $\alpha_{\varepsilon}$ = 1. These values were obtained by optimizing the initial conditions for best agreement with the experimental propane pool-like gas flame behavior, and leaving them unchanged for this work. It is possible that this approach might compensate for the lack of elliptic treatment near the flame base, and improve the near field predictions.

Combustion Rate

The chemical kinetics are assumed to be infinitely fast. However, the microscale processes responsible for the turbulence dissipation and molecular mixing in the turbulent field are typically intermittent and certainly not infinitely fast. The details of this model can be found elsewhere [7-9,11]. Within this model, the overall reaction rate is given by the expression,

$$R_{fu} = \frac{\dot{m}}{(1-\tau^* )} C_{min} \text{ (kg/m}^3\text{s)}$$

where $C_{min}$ is the smaller of $C_{fu}$ and $C_{O2}/r_{fu}$. Here, $C_{fu}$ and $C_{O2}$ are the concentrations of fuel and oxygen respectively, and $r_{fu}$ is the stoichiometric oxygen requirement for one kg of fuel. The quantity $\dot{m}$ is defined in terms of $\kappa$ and $\varepsilon$ and the kinematic isotropic viscosity $\nu$, and the fraction of the fluid contained within the fine structures $\tau^*$[7-9,11].

Radiation
The four flux model, in terms of radiation flux sums $F_z$ and $F_y$, in the axial and radial directions, is given as [7-9, 12]:

$$\frac{d}{dz}[\Gamma_z dF_z/dz] = K(F_z - E)$$  \hspace{1cm} (2)

$$y-1 \frac{d}{dy}[y\Gamma_y dF_y/dy] = K(F_y - E)$$  \hspace{1cm} (3)

where

$$\Gamma_y = y/(1+Ky) \text{ and } \Gamma_z = 1/K$$

Here, $K$ is the flux absorption coefficient (m$^{-1}$) to be defined later, and $E$ is the black body emissive power.

### Soot Formation

The phenomenological scheme proposed by Tesner et al.[13] has been incorporated here for modeling soot formation in a turbulent field. The soot formation process depends on the formation of active radical particles. From these particles, soot particles grow. The formation rate of radical nuclei is given by:

$$R_{nf} = n_0 + (f-g)n - g_0 n N \quad (\text{part/m}^3/\text{s})$$  \hspace{1cm} (4)

where $N$ is the concentration of soot particles (part/m$^3$) and $f$, $g$ and $g_0$ are constants. The spontaneous formation rate of radical nuclei, $n_0$, is expressed as:

$$n_0 = a_0 C_f \exp \left(-\frac{E}{RT}\right) \quad (\text{part/m}^3/\text{s})$$  \hspace{1cm} (5)

where $C_f$ is the concentration of fuel, $E$ is the activation energy, $T$ is the temperature, and $a_0$ is a constant. The soot formation rate is then expressed by the relation,

$$R_{nf} = m_p (a - bN) n \quad (\text{kg/m}^3/\text{s})$$  \hspace{1cm} (6)

where $m_p$ is the mass of the soot particles (kg/part), and $a$ and $b$ are constants.

The soot and radical nuclei are formed and burnt in the flame zone. The mean rate of nuclei and soot particle combustion are expressed respectively as follows:

$$R_{nc} = R_{fu} n / C_f \quad (\text{part/m}^3/\text{s})$$  \hspace{1cm} (7)

$$R_{sc} = R_{fu} C_s / C_f \quad (\text{kg/m}^3/\text{s})$$  \hspace{1cm} (8)

where $C_s$ is the soot concentration (kg/m$^3$). The constants needed for the soot calculations are taken from Ref.11, except that the particle size was increased to 200 Å.

The absorption coefficient, $k_g$, due to the gas was calculated using a weighted sum-gray gases model as reported by Smith et al.[14]. The details are reported elsewhere [8,9]. The soot absorption coefficient is evaluated by [5]

$$k_s = 3.6 C_s f_T T/C_z$$  \hspace{1cm} (9)
Table 1. Thermochemical properties of the liquid and gas phase utilized in the present calculations.

LIQUID PHASE
Molecular weight, MW_L = 154
Boiling point, T_b = 500 K
Liquid density at the boiling point, \( \rho_L = 740 \text{ kg/m}^3 \)
Specific heat, \( C_{pl} = 2090 \text{ J/kg K} \)
Heat of combustion, \( \Delta H_c = 4.3 \times 10^7 \text{ J/kg} \)
Latent heat of vaporization, \( \Delta H_L = 2 \times 10^5 \text{ J/kg} \)
Stoichiometric oxygen/fuel ratio, \( r_{fo} = 3.47 \)

GAS PHASE
Molecular weight, MW_G=28
Specific heat of fuel vapor, \( C_p = 1250 \text{ J/kg K} \)
Molecular viscosity, \( \mu_G = 15 \times 10^{-6} \text{ kg/m s} \)

where \( C_0 \) is a constant with a value of 4.64 [5], \( C_2 \) is Planck's second constant, and \( f_v \) is the soot volume fraction. The overall absorption coefficient \( (k) \) of the soot + gas mixture was estimated by the relation [1],

\[
k = k_g + k_s - k_2 k_a
\]

(10)

The flux absorption coefficient \( K=2k \) was assumed, implying an isotropic radiation intensity [12]. The source term of the enthalpy equation due to the axial and radial radiation fluxes is \( 2k (F_x + F_y - 2E) \).

The boundary conditions for the axial radiation flux sum at \( z=0 \) is of the form,

\[
F_z + p_1 \Gamma_z (dF_z/dz) = q_1
\]

(11)

where \( p_1 \) is 1/K and \( q_1 \) is the surface radiation. The radiation was assumed to be negligible at the top of the plume.

The parabolic expressions have been numerically solved by a marching technique using a modified GENMIX code. The axial radiation flux sum, \( F_z \), which is elliptic, was computed separately and the temperature field updated. We employed 45 grid nodes (floating) in the radial direction. A maximum axial step size of 0.1% of the current radius of the flame was employed.

The input thermochemical properties of the fuel and gas phase are summarized in Table 1. The data are mainly taken from Ref. 15

RESULTS AND DISCUSSION
Distribution of Species, Temperature and Axial Velocity.

The distribution of various species in the flame, along the centerline for three flames of increasing pool size is shown in Figure 1. The "surface" of the stoichiometric combustion region (indicated by St in
FIGURE 1. Concentration of fuel (F), oxygen, nitrogen, and products (CO₂ and H₂O), along the vertical flame axis for kerosene pool flames of indicated pool size.

Figure 1) is located at Z= 40, 75 and 125 cm for flames of 15, 30 and 50 cm pool diameters (i.e. St is about 2.5 times the pool diameter). This overall behavior is in agreement with the well known observations on gas flames of similar initial mass velocity or calorific output [8]. The combustion products reach a maximum at this stoichiometric point.

Axial distribution of mean temperature and axial velocities are shown in Figure 2A and B respectively. The axial distance where the temperature is a maximum is the combustion height, Zc, of the flame. The maximum temperatures (T₀) is close to 1150 K which is commonly observed with practical fires of kerosene or diesel fuel. The visible flame height, Zᵥ, is 58, 105 and 212 cm, respectively, for 15, 30 and 50 cm pool diameter fires (shown by the upward arrows in Figure 2). These heights are determined by the axial height where the temperature drops to 700 K. The experimental flame height of a kerosene pool fire of 15 cm diameter has
been reported by Burgess et al. [16] to be 68 cm. The overall trend is comparable with the flame height versus pool diameter curves shown in Hottels' review [17]. The axial velocity exhibits trends similar to the temperature, as shown in Figure 2B.

Soot Concentration and Absorption-Emission Behavior

Figure 3A shows the predicted soot concentration along the flame axis. The soot that escapes downstream (smoking) is due to the combustion limitation, in this case turbulence controlled. The jet flames studied by Magnussen [11] did not show any indication of smoking. However, because of the low initial momentum of the buoyant flames in the current fires, a part of the total soot formed appears to remain unburnt. An excellent account of the mechanism of soot emission as a function of inlet fuel mass flux, turbulence, and burner diameter is given by Kent and Wagner [18].

Figure 3B shows the local absorption coefficients calculated by taking into account the fuel vapor, gaseous products, and soot absorption and emission. Here, the absorption coefficient of the fuel vapor is taken to be 1.3 m$^{-1}$ based on the work of Brosmer and Tien [5]. However, the absorption-emission properties of cold fuel vapors in the vicinity of fuel surfaces need to be estimated with greater certainty. The maximum in the absorption occurs where the soot concentration is maximum, clearly suggesting the decisive effect of the soot loading on the total absorption.

**FIGURE 3.** Concentration of soot (A), and local absorption coefficient (B) along the vertical flame axis for the three indicated flames.

**FIGURE 4.** Variation of the net radiative heat flux (feedback) along the fuel surface for flames of the indicated pool size.
Table 2. Summary of flame characteristics and heat fluxes predicted by the present theory

<table>
<thead>
<tr>
<th>Properties</th>
<th>Pool diameter (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>15</td>
</tr>
<tr>
<td>Combustion height ((Z_c)), cm calculated</td>
<td>40</td>
</tr>
<tr>
<td>Flame height ((Z_v)), cm calculated</td>
<td>58</td>
</tr>
<tr>
<td>Theoretical power output ((Q_T)), kW</td>
<td>11</td>
</tr>
<tr>
<td>Completeness of combustion ((X_a))</td>
<td>0.75</td>
</tr>
<tr>
<td>Radiation heat flux at the center, calc. ((q_{r,0})), kW/m²</td>
<td>16.37</td>
</tr>
<tr>
<td>Radiation heat flux calc. (surface averaged) ((q_{r,s})), kW/m²</td>
<td>6.02</td>
</tr>
<tr>
<td>Convective heat feedback to fuel surface ((q_{c})), kW/m²</td>
<td>4.58</td>
</tr>
<tr>
<td>Gasification flux requirement ((q_{g})), kW/m²</td>
<td>1.49</td>
</tr>
<tr>
<td>Feedback flux, total calculated ((q_{fd,t})), kW/m²</td>
<td>9.18</td>
</tr>
<tr>
<td>Mass burning rate ((m^\prime)), g/m²s</td>
<td>Calculated, reported [15]</td>
</tr>
<tr>
<td></td>
<td>14.69</td>
</tr>
<tr>
<td></td>
<td>14.80</td>
</tr>
<tr>
<td>Radiative fraction ((X_r))</td>
<td>0.23</td>
</tr>
</tbody>
</table>

\[ q_{rr} = \varepsilon_s \sigma T_s^4, \]  

(13)

where \(\sigma\) is the Stefan-Boltzmann constant, \(T_s\) is the fuel surface temperature, and \(\varepsilon_s\) is the surface emissivity, which is taken as 0.42 for kerosene [15].

A representative analysis of the thermal radiation behavior for a pool flame of 30 cm diameter is given here. The radiative heat flux at the center, \(q_{r,0}\), is 20.18 kW/m² for this pool. However as explained earlier, the surface averaged flux \(q_{r,s}\) is far lower, namely 13.30 kW. (see Table 2 for these values). The gasification flux requirement \(q_{g}\) is 13.77 kW/m²; this is an experimentally measured quantity based on the fact that \(m^\prime\) is measured [16]. By the energy balance equation (Eq. (11)), \(m^\prime\) is calculated. Here, \(m^\prime = 22.22\) g/m²s is obtained for the \(D=30\) cm pool fire. The reported value is 22.01 [15]. However, for larger pool sizes, the predicted feedback energy is underestimated. This might arise because some of the physical parameters (such as the combustion efficiency, emissivity etc.) are not optimized for larger scale fires.

Total Radiation Output

The total radiation output \((Q_{ext})\) from the flame is an important quantity which determines the extent of thermal damage by the fire. The radiative fraction, \(X_r\), is a parameter that represents the fraction of the
and emission processes. The magnitude of the predicted absorption coefficients are comparable to the recent experimental values reported by Markstein [4] on propane flames. The local emissivity (not shown here) follows a similar trend. One of the significant theoretical observations of this study is the quantitative increase of the soot formation, local absorption coefficients, and emissivity of the pool flames with increasing pool size.

Radiative Feedback

The radiative heat feedback to the fuel surface is an important quantity of interest to burning rate calculations. The radial distribution of the radiative heat flux to the fuel surface, for pool fires of increasing size, are shown in Figure 4. The present observation indicates that the core properties of the flame play a dominant role in the feedback process. As the pool size increases, the flux at the center decreases (from bottom to top in this Figure). The heat flux curve has a maximum about midway along the radius. It appears that the flame envelope gets farther from the flame axis at larger fire scale, hence the cold fuel vapor and soot markedly block the radiative feedback at the center. This response has been reported recently by Brosmer and Tein [5] for a PMMA pool fire. The mass loss rate in these cases is the surface averaged quantity.

Analysis of Thermal Radiation Behavior

From the results shown above, the mass burning rate can be computed using the surface averaged radiative heat flux, \( \dot{q}_{rs} \), and the energy balance for the liquid/vapor interface:

\[
\dot{q}_{rs} + \dot{q}_{c} = m' \left[ \Delta H_L + \frac{C_p(T_s - T_a)}{2L} \right] + \dot{q}_{rr} + \dot{q}_r
\]

(11)

Here, the terms I and II refer to the radiant and convective heat fluxes, respectively, to the surface of the liquid pool. The sum of these quantities is balanced by the vaporization flux requirement (term III), plus the re-radiated heat loss from the surface (term IV) and the conductive heat flux (term V) to the liquid pool. The values of the various terms indicated here have been evaluated and summarized in Table 2 for three pool sizes.

A brief account of the methods used to estimate the terms follows. The convective heat flux, \( \dot{q}_c \), is calculated using the relation [1]:

\[
\dot{q}_c = \left( \frac{h}{C_p} \right) [ \Delta H_L (X_a - X_f) - (1/0.232) \Delta H_v X_a] - \frac{C_p(T_s - T_a)}{h} f(p)
\]

(12)

where \( f(p) = p/(e^p - 1) \) and \( p = \dot{m}' C_p / h \). A value of \( \frac{h}{C_p} = 0.01 \text{ kg/m}^2\text{s} \) was utilized along with the other properties defined in Table 1 and 2 to compute \( \dot{q}_c \) for all the flames. Table 2 shows that the convective contribution decreases from 54 to 5% as the pool size increases from 15 to 50 cm, thereby showing the importance of radiation in larger scale fires. The heat loss due to conductive heat transfer into the liquid phase is neglected in this work and the re-radiated radiation flux is computed by the relation,
energy released by combustion which is emitted from the flame by thermal radiation \((X_r = \frac{Q_{ext}}{Q_b})\). \(Q_{ext}\) is computed from the relation,

\[
Q_{ext} = 2 \pi \int_0^{Z_p} Y_{fls} \, Q_{fls} \, dz
\]  

The term on the right hand side above represents the integral of the radiation loss from the lateral surface. Here \(Y_{fls}\) and \(Q_{fls}\) are the lateral coordinate and heat output at the flame surface respectively. The calculations give a value of \(X_r = 0.23, 0.32, \) and \(0.43\) for the 15, 30 and 50 cm pool flames, which are comparable to those generally reported for open pool fires [15].

CONCLUSIONS

The pool fire characteristics of kerosene with moderate to large pool size have been investigated. The overall behavior of the predicted flame lengths and flame temperatures are reasonably close to experimental values.

The predicted soot formation behavior indicates that unlike in high initial momentum jet flames, the present fires exhibit a significant smoking tendency at the flame tip. This behavior in turn affects the radiative heat transfer. The important observation, which is consistent with previous experiment data on pool fires, is that the tendency to soot increases with pool size.

A comprehensive account of the role of thermal radiation in pool fires is described by a non-homogeneous, non-isothermal radiation model. This study provides some basic understanding of the heat transfer behavior in practical pool fires of kerosene, aspects which are beyond the scope of zone models. Considerable radiation energy blockage by the cold fuel vapor and soot formed in fires of larger size gives rise to a significantly variable heat flux distribution at the fuel surface which in turn yields a non-uniform mass burning rate.

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REFERENCES


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